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Nodal lines of random eigenfunctions of the Laplacian

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In this talk I will introduce the audience to nodal lines. The nodal lines were first discovered by the German physicist, musician and philosopher Ernst Chladni as the mysterious shapes appearing on musical instruments or highly excited membrane, varying with the membrane and the frequency.

Given a surface, one considers the zeros of the eigenfunctions of the Laplacian associated to large eigenvalues. In this situation it is widely accepted to model the nodal lines using Berry's random wave model. For surfaces like the torus or the sphere, one can use the multiplicities in the spectrum to endow the eigenspaces with Gaussian probability measure, and study the statistical properties of the corresponding nodal lines.

Joint with Zeev Rudnick, Andrew Granville, John Toth and Manjunath Krishnapur.