Information processing devices that can manipulate quantum states have the potential to perform several interesting computing feats. I will focus on some of the remarkable properties of entangled quantum states, and show that they can be cast in a setting that raises questions about the soundness of certain mathematical proof systems.